

Geometry

U-46 Curriculum Scope and Sequence

| Reporting Strand | Instructional Focus | Common Core Standards | Pacing |
|---------------------------------------|---|---|-----------|
| Geometric Transformations | 1.1 Explore building blocks of geometry | <u>G.CO.1</u> | 5 weeks |
| | 2.1 Explore with transformations | G.CO.2, G.CO.3, G.CO.4, G.CO.5 | |
| | 2.2 Investigate and apply congruence definitions | G.CO.6, G.CO.7 | |
| Coordinate Plane & Intersecting Lines | 1.2 Explore coordinate plane | G.GPE.4, G.GPE.6, G.GPE.7 | 5 weeks |
| | 1.3 Explore congruence constructions | G.CO.12, G.GPE.4 | |
| | 3.1 Explore parallel and perpendicular lines | G.CO.12, <u>G.GPE.5</u> | |
| | 3.2 Prove theorems about lines and angles | G.GPE.4, <u>G.CO.9</u> | |
| Triangle Geometry (Congruence) | 4.1 Prove congruence theorems | G.CO.8, <u>G.CO.10</u> , G.SRT.5 | 4 weeks |
| | 4.2 Construct special triangles and angles | G.CO.9, G.CO.12, G.CO.13 | |
| Similarity | 5.1 Use dilations to show figures similar. | G.SRT.1, G.SRT.2 | 4 weeks |
| | 5.2 Explain and prove similarity theorems | <u>G.CO.10</u> , G.SRT.3, <u>G.SRT.4</u> , <u>G.SRT.5</u> , G.MG.3 | |
| | 5.3 Apply similarity theorems (Extension Honors Only) | G.SRT.2, G.SRT.5 | |
| Trigonometry | 6.1 Investigate right triangle trigonometry | <u>G.SRT.6</u> , <u>G.SRT.7</u> , <u>G.SRT.8</u> | 3 weeks |
| | 6.2 Solve applied problems involving trigonometry (Extension Honors only) | G.SRT.10, G.SRT.11, N.Q.3, G.MG.3 | |
| Circles | 7.1-2 Investigate circles and apply formulas | G.C.1, <u>G.C.2</u> , G.C.4, <u>G.C.5</u> , G.GMD.1 | 6 weeks |
| | 7.3 Investigate and interpret circle equations | <u>G.GPE.1</u> , G.GPE.4 | |
| | 8.1 Investigate concurrency in triangles | <u>G.CO.10</u> , <u>G.C.3</u> | |
| Quadrilaterals & Other Polygons | 9.1 Construct and explore polygons | G.CO.13, <u>G.C.3</u> | 4 weeks |
| | 9.2 Prove and apply theorems about quadrilaterals | G.CO.11, G.GPE.4 | |
| 3-D Figures | 10.1 Investigate cross sections and rotations | G.GMD.4, G.MG.1, G.MG.3 | 3-4 weeks |
| | 10.2 Develop and apply volume formulas | G.MG.1, <u>G.MG.2</u> , G.MG.3, G.GMD.1, G.GMD.2, <u>G.GMD.3</u> | |

Standards that are **bolded and underlined** are the essential “power standards” for SAT

Geometric Transformations

1.1 Explore building blocks of geometry

| CCSS | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|--|--|--|--|--|
| Definitions of lines and angles (G.CO.1) | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p>Describe the following terms using points, lines, distance and circular arcs for all of the following:</p> <ul style="list-style-type: none"> • Angles • Circles • Perpendicular Lines • Parallel Lines • Line Segments | <p>Describe the following terms using points, lines, distance and circular arcs for 4 of the following:</p> <ul style="list-style-type: none"> • Angles • Circles • Perpendicular Lines • Parallel Lines • Line Segments | <p>Describe the following terms using points, lines, distance and circular arcs for 2 of the following:</p> <ul style="list-style-type: none"> • Angles • Circles • Perpendicular Lines • Parallel Lines • Line Segments | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |

G.CO.1 Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc.

This standard may be reassessed in other reporting strands, as concepts are developed and taught.

Geometric Transformations

2.1 Explore with transformations

| CCSS | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|--|---|--|--|--|
| Represent, describe and compare transformations (G.CO.2, G.CO.5) | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p>Draw and describe transformations of reflections, rotations, translations, and combinations of these, including mapping a figure onto another.</p> <p>Describe reflections, translations, and rotations as functions that take points on the plane as inputs and give other points as outputs</p> <p>Compare transformations that preserve distance and angles to those that do not</p> | <p>Draw or describe transformations of reflections, rotations, translations, and a combination of these, including mapping a figure onto another.</p> <p>Describe reflections and translations as functions that take points on the plane as inputs and give other points as outputs</p> <p>Describe transformations that preserve distance and angles to those that do not</p> | <p>Draw and describe a singular transformation of reflections and translations, including mapping a figure onto another.</p> <p>Given a function rule for reflections and translations, identify the outputs</p> <p>Identify transformations that preserve distance and angles to those that do not</p> | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |
| | | <p>Describe and illustrate rotations and reflections of a rectangle, parallelogram, trapezoid, or regular polygon that carry each figure onto itself.</p> | <p>Describe or illustrate rotations and reflections of a rectangle, parallelogram, trapezoid, or regular polygon that carry each figure onto itself.</p> | <p>Describe or illustrate rotations or reflections of a rectangle, parallelogram, trapezoid, or regular polygon that carry each figure onto itself.</p> | |
| | | <p>Develop the definition of all the terms rotations, reflections and translations in terms of:</p> <ul style="list-style-type: none"> • Angles • Circles • Perpendicular lines • Parallel lines • Line segments. | <p>Develop the definition for 4 of the terms rotations, reflections and translations in terms of:</p> <ul style="list-style-type: none"> • Angles • Circles • Perpendicular lines • Parallel lines • Line segments. | <p>Develop the definition for 2 of the terms rotations, reflections and translations in terms of:</p> <ul style="list-style-type: none"> • Angles • Circles • Perpendicular lines • Parallel lines • Line segments. | |
| Describe symmetry (G.CO.3) | | | | | |
| Develop definitions of transformations (G.CO.4) | | | | | |

G.CO.2 Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch).

G.CO.5 Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another.

G.CO.3 Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself.

G.CO.4 Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments.

Geometric Transformations

2.2 Investigate and apply congruence definitions

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|--|--|---|---|---|--|
| <p>Predict and decide congruency (G.CO.6)</p> <p>Corresponding sides and angles (G.CO.7)</p> | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p>Use descriptions of rigid motions to predict the effect of a rigid motions on a figure</p> <p>Use the definition of congruence in terms of rigid motions to:</p> <ul style="list-style-type: none"> • decide if two given figures are congruent • prove that corresponding sides are congruent and corresponding angles are congruent in a pair of congruent triangles | <p>Use descriptions of rigid motions to show the effect of a rigid motions on a figure</p> <p>Use the definition of congruence in terms of rigid motions to:</p> <ul style="list-style-type: none"> • decide if two given figures are congruent • show that corresponding sides are congruent and corresponding angles are congruent in a pair of congruent triangles | <p>Use descriptions of rigid motions to identify the effect of a rigid motions on a figure</p> <p>Use the definition of congruence in terms of rigid motions to:</p> <ul style="list-style-type: none"> • decide if two given figures are congruent • identify that corresponding sides are congruent and corresponding angles are congruent in a pair of congruent triangles | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |

G.CO.6 Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.

G.CO.7 Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent.

Coordinate Plane and Intersecting Lines

1.2 Explore coordinate plane

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|--|---|--|--|---|--|
| Find the point (G.GPE.6) | Can extend thinking beyond the standard, including tasks that may involve one of the following: | Find the point on a line segment, given two endpoints that divide <u>the segment into a given ratio.</u> | Find the point on a line segment, given two endpoints, that divides a <u>horizontal or vertical segment into a given ratio.</u> | Find the point on a line segment, given two endpoints, that divides the <u>segment in half.</u> | Little evidence of reasoning or application to solve the problem |
| Prove using formulas (G.GPE.4) Perimeter and area (G.GPE.7) | <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | Using coordinate geometry and the Pythagorean, slope, distance and midpoint formulas to do <u>both</u> of the following <ul style="list-style-type: none"> • find the perimeter of polygons. • find the area <u>of polygons using</u> triangles and rectangles | Using coordinate geometry and the Pythagorean, slope, distance and midpoint formulas to do <u>both</u> of the following <ul style="list-style-type: none"> • find the perimeter of polygons. • find the area of triangles and rectangles | Using coordinate geometry and the Pythagorean, slope, distance and midpoint formulas to do <u>one</u> of the following <ul style="list-style-type: none"> • find the perimeter of polygons. • find the area of triangles and rectangles | Does not meet the criteria in a level 1 |

G.GPE.4 Use coordinates to prove simple geometric theorems algebraically. For example, prove or disprove that a figure defined by four given points in the coordinate plane is a rectangle; ~~prove or disprove that the point $(1, \sqrt{3})$ lies on the circle centered at the origin and containing the point $(0, 2)$.~~

G.GPE.7 Use coordinates to compute perimeters of polygons and areas of triangles and rectangles, e.g., using the distance formula. ★

G.GPE.6 Find the point on a directed line segment between two given points that partitions the segment in a given ratio.

Embedded standard not summatively assessed.

G.CO.1 Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc.

Coordinate Plane and Intersecting Lines

1.3 Explore congruence constructions

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|---|--|--|--|---|
| Construction of lines and angles (G.CO.12) | Can extend thinking beyond the standard, including tasks that may involve one of the following: | Use a variety of tools to perform both of the following with precision : <ul style="list-style-type: none"> • copy a segment • copy an angle | Use a variety of tools to perform both of the following: <ul style="list-style-type: none"> • copy a segment • copy an angle | Use a variety of tools to perform 1 of the following: <ul style="list-style-type: none"> • copy a segment • copy an angle | Little evidence of reasoning or application to solve the problem Does not meet the criteria in a level 1 |
| Prove using formulas (G.GPE.4) | <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | Using coordinate geometry and the slope, distance and midpoint formulas to prove all of the following <ul style="list-style-type: none"> • Segments on a coordinate plane are congruent • Segments on a coordinate plane are perpendicular • Segments on a coordinate plane are parallel | Using coordinate geometry and the slope, distance and midpoint formulas to prove two of the following <ul style="list-style-type: none"> • Segments on a coordinate plane are congruent • Segments on a coordinate plane are perpendicular • Segments on a coordinate plane are parallel | Using coordinate geometry and the slope, distance and midpoint formulas to prove one of the following <ul style="list-style-type: none"> • Identify if segments on a coordinate plane are congruent • Identify If segments on a coordinate plane are perpendicular • Segments on a coordinate plane are parallel | |

G.CO.12 Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometric software, etc.). Copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment; and constructing a line parallel to a given line through a point not on the line.

G.GPE.4 Use coordinates to prove simple geometric theorems algebraically.

Coordinate Plane and Intersecting Lines

3.1 Explore parallel and perpendicular lines

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|--|---|--|---|--|
| Construction of lines and angles (G.CO.12) | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p>Use a variety of tools and methods to perform both of the following with precision:</p> <ul style="list-style-type: none"> • Construct perpendicular lines • Construct a line parallel to a given line through a point not on the line. | <p>Use a variety of tools and methods to perform both of the following:</p> <ul style="list-style-type: none"> • Construct perpendicular lines • Construct a line parallel to a given line through a point not on the line. | <p>Use a variety of tools and methods to perform one of the following:</p> <ul style="list-style-type: none"> • Construct perpendicular lines • Construct a line parallel to a given line through a point not on the line. | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |
| Prove and use parallel and perpendicular lines (G.GPE.5) | | <p>Prove a pair of lines are parallel or perpendicular using slope</p> <p>Write the equation of a line that is parallel and perpendicular to a given line that passes through a given point</p> | <p>Given the slope of 1 line, prove if a pair of lines are parallel or perpendicular</p> <p>Write the equation of a line that is parallel or perpendicular to a given line that passes through a given point</p> | <p>Given the slope of a pair of lines, identify the lines are parallel or perpendicular</p> <p>Identify the equation of a line that is parallel or perpendicular to a given line that passes through a given point</p> | |

G.CO.12 Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometric software, etc.). Copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment; and constructing a line parallel to a given line through a point not on the line.

G.GPE.5 Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point).

Embedded standard not summatively assessed.

G.CO.1 Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc.

Coordinate Plane and Intersecting Lines

3.2 Prove theorems about lines and angles

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|--|---|---|---|--|
| Prove lines and angles (G.CO.9, G.GPE.4) | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p>Prove all of the following theorems</p> <ul style="list-style-type: none"> • Vertical angles are congruent. • When a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent | <p>Show mathematically all of the following theorems</p> <ul style="list-style-type: none"> • Vertical angles are congruent. • When a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent | <p>Identify all of the following</p> <ul style="list-style-type: none"> • Vertical angles are congruent. • When a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |

G.GPE.4 Use coordinates to prove simple geometric theorems algebraically. For example, prove or disprove that a figure defined by four given points in the coordinate plane is a rectangle; ~~prove or disprove that the point $(1, \sqrt{3})$ lies on the circle centered at the origin and containing the point $(0, 2)$.~~

G.CO.9 Prove theorems about lines and angles. Theorems include: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent; points on a perpendicular bisector of a line segment are exactly those equidistant from the segment’s endpoints.

Embedded standard not summatively assessed. This concept can be used as a reassessment opportunity.

G.GPE.5 Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point).

Triangle Geometry

4.1 Prove congruence theorems

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|--|---|---|--|---|---|
| Explain triangle congruence (G.CO.8) | Can extend thinking beyond the standard, including tasks that may involve one of the following: | Prove SSS, SAS, and ASA triangle congruence using rigid motion. | Identify all SSS, SAS, ASA, AAS, and HL triangle congruence <u>using rigid motion</u> | Identify if triangles are congruent and by which method (SSS, SAS, ASA, AAS or HL) | Little evidence of reasoning or application to solve the problem Does not meet the criteria in a level 1 |
| Prove triangle theorems (G.CO.10) | <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | Prove both of the following theorems <ul style="list-style-type: none"> • measures of interior angles of a triangle sum to 180° • base angles of isosceles triangles are congruent | Prove one of the following theorems <ul style="list-style-type: none"> • measures of interior angles of a triangle sum to 180° • base angles of isosceles triangles are congruent | Use the following theorems to mathematically solve for missing angles <ul style="list-style-type: none"> • measures of interior angles of a triangle sum to 180° • base angles of isosceles triangles are congruent | |
| Solve and prove relationships (G.SRT.5) | | Solve and prove geometric problems using congruence criteria | Solve and prove geometric problems, given a proof frame , using congruence criteria | Solve geometric problems using congruence criteria | |

G.CO.8 Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions.

G.CO.10 Prove theorems about triangles. Theorems include: measures of interior angles of a triangle sum to 180° ; base angles of isosceles triangles are congruent; ~~the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length;~~ ~~the medians of a triangle meet at a point.~~

G.SRT.5 Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures.

Triangle Geometry

4.2 Construct special triangles and angles

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|--|--|---|---|---|--|
| Construction of lines and angles (G.CO.12, G.CO.13, G.CO.9) | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p>Use a variety of tools to perform all of the following:</p> <ul style="list-style-type: none"> • Bisect a segment • Bisect an angle • Construct the perpendicular bisector of a segment • Construct an equilateral triangle | <p>Use a variety of tools to perform 3 of the following:</p> <ul style="list-style-type: none"> • Bisect a segment • Bisect an angle • Construct the perpendicular bisector of a segment • Construct an equilateral triangle | <p>Use a variety of tools to perform 2 of the following:</p> <ul style="list-style-type: none"> • Bisect a segment • Bisect an angle • Construct the perpendicular bisector of a segment • Construct an equilateral triangle | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |

G.CO.9 Prove theorems about lines and angles: points on a perpendicular bisector of a line segment are exactly those equidistant from the segment’s endpoints.

G.CO.13 Construct an equilateral triangle, a square, and a regular hexagon inscribed in a circle.

G.CO.12 Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometric software, etc.). Copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment; and constructing a line parallel to a given line through a point not on the line.

Similarity

5.1 Use dilations to show figures similar

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|--|--|--|---|---|--|
| <p>Properties of Dilations (G.SRT.1)</p> <p>Explain similarity (G.SRT.2)</p> | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p>Verify that when a side passes through the center of dilation, <u>the side and its image lie on the same line.</u></p> <p>Verify that corresponding sides of the pre-image and images are <u>parallel and</u> proportional after dilation.</p> <p>Explain <u>using transformations</u> if two figures are similar by verifying</p> <ul style="list-style-type: none"> • corresponding angles are congruent • corresponding sides are proportional | <p>Given an image and the pre-image, <u>determine the center of dilation</u></p> <p>Verify that corresponding sides of the pre-image and images are <u>proportional by finding the scale factor.</u></p> <p>Explain if two figures are similar by verifying</p> <ul style="list-style-type: none"> • corresponding angles are congruent • corresponding sides are proportional | <p>Perform dilation with a given center and scale factor on a figure in the coordinate plane.</p> <p>Show mathematically if two figures are similar by verifying</p> <ul style="list-style-type: none"> • corresponding angles are congruent • corresponding sides are proportional | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |

G.SRT.1 Verify experimentally the properties of dilations given by a center and a scale factor:

- dilation takes a line not passing through the center of the dilation to a parallel line, and leaves a line passing through the center unchanged.
- the dilation of a line segment is longer or shorter in the ratio given by the scale factor.

G.SRT.2 Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides.

Similarity

5.2 Explain and prove similarity theorems

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|--|---|--|--|--|---|
| Prove similar triangles (G.SRT.3) | Can extend thinking beyond the standard, including tasks that may involve one of the following: <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | Prove all using transformations of the following theorems: <ul style="list-style-type: none"> • Angle-Angle (AA) criterion for two triangles to be similar • SAS for two triangles to be similar • SSS for two triangles to be similar | Prove two using transformations of the following theorem: <ul style="list-style-type: none"> • AA criterion for two triangles to be similar • SAS for two triangles to be similar • SSS for two triangles to be similar | Identify if triangles are similar by: <ul style="list-style-type: none"> • AA~ • SAS~ • SSS~ | Little evidence of reasoning or application to solve the problem Does not meet the criteria in a level 1 |
| Solve and prove relationships (G.SRT.5, G.MG.3) | | Solve and prove real world geometric problems using congruence and similarity | Solve real world geometric problems using congruence and similarity | Solve mathematical geometric problems using congruence and similarity | |
| Prove triangle theorems (G.SRT.4, G.CO.10) | | Prove all of the following theorems: <ul style="list-style-type: none"> • a line parallel to one side of a triangle divides the other two proportionally • if a line divides two sides of a triangle proportionally; then it is parallel to the third side. • Pythagorean Theorem proved using triangle similarity | Prove 2 of the following theorems: <ul style="list-style-type: none"> • a line parallel to one side of a triangle divides the other two proportionally • if a line divides two sides of a triangle proportionally; then it is parallel to the third side. • Pythagorean Theorem proved using triangle similarity | Prove 1 of the following theorems: <ul style="list-style-type: none"> • a line parallel to one side of a triangle divides the other two proportionally • if a line divides two sides of a triangle proportionally; then it is parallel to the third side. • Pythagorean Theorem proved using triangle similarity | |

G.SRT.3 Use the properties of similarity transformations to establish the AA criterion for two triangles to be similar.

G.SRT.5 Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures.

G.SRT.4 Prove theorems about triangles. Theorems include: a line parallel to one side of a triangle divides the other two proportionally, and conversely; the Pythagorean Theorem proved using triangle similarity.

G.CO.10 Prove theorems about triangles. Theorems include: ~~measures of interior angles of a triangle sum to 180°; base angles of isosceles triangles are congruent;~~ the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; ~~the medians of a triangle meet at a point.~~

G.MG.3 Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios). ★

Similarity

5.3 Apply similarity theorems (Extension – Honors Only)

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|--|--|--|--|--|--|
| Solve and prove relationships (G.SRT.5) | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | Solve and prove geometric problems using congruence and similarity | Solve geometric problems using congruence and similarity | Solve geometric problems using congruence or similarity | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |
| Explain similarity (G.SRT.2) | | <p>Verify that corresponding sides of the pre-image and images are parallel and proportional after dilation.</p> <p>Explain using transformations if two figures are similar by verifying</p> <ul style="list-style-type: none"> • corresponding angles are congruent • corresponding sides are proportional | <p>Verify that corresponding sides of the pre-image and images are proportional by finding the scale factor.</p> <p>Explain if two figures are similar by verifying</p> <ul style="list-style-type: none"> • corresponding angles are congruent • corresponding sides are proportional | <p>Show mathematically if two figures are similar by verifying</p> <ul style="list-style-type: none"> • corresponding angles are congruent • corresponding sides are proportional | |

G.SRT.5 Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures.

G.SRT.2 Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides.

Trigonometry

6.1 Investigate right triangle trigonometry

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|--|--|--|---|---|--|
| <p>Understand side ratios (G.SRT.6)</p> <p>Use sine and cosine (G.SRT.7)</p> | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p>Use properties of similar right triangles to form the definitions of</p> <ul style="list-style-type: none"> • sine • cosine • tangent <p><u>Explain and use the relationship between the sine of an acute angle and the cosine of its complement.</u></p> | <p><u>Use side ratios</u> to prove angles are congruent between triangles leading to similar triangles.</p> | <p><u>Find the trig ratios</u> of a given right triangle.</p> | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |
| <p>Use Trig Ratios (G.SRT.8)</p> | | <p>Use trigonometric ratios and the Pythagorean Theorem in applied problems to find</p> <ul style="list-style-type: none"> • unknown sides • unknown angles | <p><u>Given an image</u>, use trigonometric ratios <u>and the Pythagorean Theorem in applied problems</u> to find</p> <ul style="list-style-type: none"> • unknown sides • unknown angles | <p><u>Given an image</u>, solve right triangles using trigonometric ratios for:</p> <ul style="list-style-type: none"> • unknown sides • unknown angles | |

G.SRT.6 Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles.

G.SRT.7 Explain and use the relationship between the sine and cosine of complementary angles.

G.SRT.8 Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems. ★

Trigonometry

6.2 Solve applied problems involving trigonometry (Honors Only)

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|-----------------------------------|--|--|--|--|--|
| G.SRT.10, G.SRT.11, G.MG.3 | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p><u>Prove the Law of Sines and the Law of Cosines,</u> and apply them to find unknown measurements in oblique triangles <u>and interpret solutions in context of real-world situations</u></p> | <p><u>Apply the Law of Sines and the Law of Cosines to find unknown measurements in oblique triangles</u></p> | <p>Identify whether the Law of Sines or the Law of Cosines should be applied to an oblique triangle to find unknown measurements, and if the ambiguous case applies to the triangle.</p> | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |

G.SRT.10 (+) Prove the Laws of Sines and Cosines and use them to solve problems.

G.SRT.11 (+) Understand and apply the Law of Sines and the Law of Cosines to find unknown measurements in right and non-right triangles (e.g., surveying problems, resultant forces).

G.MG.A.3 Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).*

Circles

7.1-7.2 Investigate circles and apply formulas

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|---|---|---|--|---|
| Circle relationships (G.C.2) | Can extend thinking beyond the standard, including tasks that may involve one of the following: <ul style="list-style-type: none"> Designing Connecting Synthesizing Applying Justifying Critiquing Analyzing Creating Proving | Describe and use the relationship to calculate values for all of the following : <ul style="list-style-type: none"> central angle inscribed angle circumscribed angles inscribed angles on a diameter angle formed by the radius of a circle and a tangent | Describe and use the relationship to calculate values for 4 of the following: <ul style="list-style-type: none"> central angle inscribed angle circumscribed angles inscribed angles on a diameter angle formed by the radius of a circle and a tangent | Use the relationship to calculate values for 3 of the following : <ul style="list-style-type: none"> central angle inscribed angle circumscribed angles inscribed angles on a diameter angle formed by the radius of a circle and a tangent | Little evidence of reasoning or application to solve the problem Does not meet the criteria in a level 1 |
| Prove and explain (G.C.1, G.C.5) | | Use similarity to prove : <ul style="list-style-type: none"> Circles are similar using transformations The length of the arc intercepted by an angle is proportional to the radius <p>Define the radian measure of the angle as the constant of proportionality</p> <p>Derive and explain the formula for the area of a sector</p> | Use similarity to do all of the following: <ul style="list-style-type: none"> Prove circles are similar using transformations Calculate the length of an arc <p>Calculate a radian measure when given an arc length and its radius.</p> <p>Given the area of a sector, find the radius</p> | Use similarity to do one of the following: <ul style="list-style-type: none"> Prove circles are similar using transformations Calculate the length of an arc <p>Convert degrees to radians using the constant of proportionality</p> <p>Find the area of a sector</p> | |
| G.GMD.1 | | Give an informal argument for the formulas for the circumference of a circle and area of a circle | Give an informal argument for the formulas for the circumference of a circle or area of a circle | Use formulas for circumference and area of a circle to solve problems | |
| Constructions (G.C.4) | | Construct a tangent line from a point outside a given circle to a circle with precision. | Construct a tangent line from a point outside a given circle to a circle. | Construct a tangent line from a point on a circle. | |

G.C.1 Prove that all circles are similar.

G.C.2 Identify and describe relationships among inscribed angles, radii, and chords. *Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle.*

G.C.3 Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle.

G.C.4 Construct a tangent line from a point outside a given circle to the circle.

G.C.5 Derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector.

G.GMD.1 Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. Use dissection arguments, Cavalieri's principle, and informal limit arguments

Circles

7.3 Investigate and interpret circle equations.

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|--|--|---|--|--|
| Derive the equation (G.GPE.1, GPE.4) | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p>Explain why the Pythagorean Theorem can be used to derive the equation of a circle, given the center and radius</p> <p>Complete the square when a is greater than 1 to find the center and radius of a circle when given an equation of a circle.</p> <p>Justify whether a point lies on a circle given the center and a point on the circle.</p> | <p>Use the Pythagorean theorem to find the equation of a circle</p> <p>Complete the square when a equals 1 to find the center and radius of a circle when given an equation of a circle.</p> <p>Determine whether a point lies on a circle given the center of the circle and the radius.</p> | <p>Use the Pythagorean theorem to find the radius of a circle</p> <p>Given guided steps, complete the square when a equals 1 to find the center and radius of a circle when given an equation of a circle.</p> <p>Given the equation determine whether a point lies on a circle.</p> | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |

G.GPE.1 Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation.

G.GPE.4 Use coordinates to prove simple geometric theorems algebraically. ~~For example, prove or disprove that a figure defined by four given points in the coordinate plane is a rectangle; prove or disprove that the point $(1, \sqrt{3})$ lies on the circle centered at the origin and containing the point $(0, 2)$.~~

Circles

8.1 Concurrency in Triangles

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|---|--|---|--|---|
| Concurrency in Triangles (G.CO.10) | Can extend thinking beyond the standard, including tasks that may involve one of the following: <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <u>Prove</u> the medians of a triangle meet at a point. | <u>Use constructions to show</u> the medians of a triangle meet at a point. | <u>Identify</u> the properties of a centroid | Little evidence of reasoning or application to solve the problem Does not meet the criteria in a level 1 |
| Constructions (G.C.3) | | Construct <u>both</u> of the following: <ul style="list-style-type: none"> • the inscribed circle of a triangle. • the circumscribed circle of a triangle. | Construct <u>one</u> of the following: <ul style="list-style-type: none"> • the inscribed circle of a triangle. • the circumscribed circle of a triangle. | <u>Identify</u> the following: <ul style="list-style-type: none"> • incenter is the intersection of the angle bisectors • circumcenter is the intersection perpendicular bisectors | |

G.C.3 Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle.

G.CO.10 Prove theorems about triangles. Theorems include: measures of interior angles of a triangle sum to 180° ; base angles of isosceles triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point.

Quadrilaterals and Other Polygons

9.1 Construct and explore polygons

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|---|---|---|--|---|
| Construct triangles and hexagons (G.CO.13) | Can extend thinking beyond the standard, including tasks that may involve one of the following: <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | Construct an inscribed regular hexagon and an inscribed square | Construct an <u>inscribed regular hexagon or an inscribed square</u> | Construct a square given a side | Little evidence of reasoning or application to solve the problem Does not meet the criteria in a level 1 |
| Prove quadrilateral properties (G.C.3) | | <u>Prove</u> properties of angles for a quadrilateral inscribed in a circle. | <u>Show mathematically</u> properties of angles for a quadrilateral inscribed in a circle. | <u>Identify</u> properties of angles for a quadrilateral inscribed in a circle. | |

G.CO.13 Construct an equilateral triangle, a square, and a regular hexagon inscribed in a circle.

G.C.3 Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle.

Quadrilaterals and Other Polygons

9.2 Prove theorems about quadrilaterals

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|--|---|---|--|--|
| Prove parallelogram theorems (G.CO.11) | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p>Prove all of the following theorems about parallelograms</p> <ul style="list-style-type: none"> • opposite sides are congruent, • opposite angles are congruent, • the diagonals of a parallelogram bisect each other, • rectangles are parallelograms with congruent diagonals | <p>Show mathematically all of the following theorems about parallelograms</p> <ul style="list-style-type: none"> • opposite sides are congruent, • opposite angles are congruent, • the diagonals of a parallelogram bisect each other, • rectangles are parallelograms with congruent diagonals | <p>Identify all of the following theorems about parallelograms</p> <ul style="list-style-type: none"> • opposite sides are congruent, • opposite angles are congruent, • the diagonals of a parallelogram bisect each other, • rectangles are parallelograms with congruent diagonals | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |
| Prove with coordinates (G.GPE.4) | | Using coordinate geometry and the Pythagorean, slope, distance, and midpoint formulas to prove the types of quadrilaterals | Using coordinate geometry and the Pythagorean, slope, distance, and midpoint formulas to identify the types of quadrilaterals | Using coordinate geometry and the Pythagorean, slope, distance, and midpoint formulas to identify properties of quadrilaterals | |

G.CO.11 Prove theorems about parallelograms. Theorems include: opposite sides are congruent, opposite angles are congruent, the diagonals of a parallelogram bisect each other, and conversely, rectangles are parallelograms with congruent diagonals.

G.GPE.4 Use coordinates to prove simple geometric theorems algebraically. For example, prove or disprove that a figure defined by four given points in the coordinate plane is a rectangle; prove or disprove that the point $(1, \sqrt{3})$ lies on the circle centered at the origin and containing the point $(0, 2)$.

3D Figures

10.1 Investigate Cross Sections and Rotations

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|---|---|--|---|---|
| Identify objects (G.GMD.4) | Can extend thinking beyond the standard, including tasks that may involve one of the following: <ul style="list-style-type: none"> • Designing • Connecting • Synthesizing | Identify the shapes of two dimensional cross sections of three dimensional objects and identify three dimensional objects generated by rotations of two dimensional objects. | Identify the shapes of two dimensional cross sections of three dimensional objects or identify three dimensional objects generated by rotations of two dimensional objects. | | Little evidence of reasoning or application to solve the problem Does not meet the criteria in a level 1 |
| Use Shapes (G.MG.1} Solve design problems (G.MG.3) | <ul style="list-style-type: none"> • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | Describe objects in context of a situation using geometric shapes their measures, and properties and use them to solve problems related to | Describe objects in context of a situation using geometric shapes, their measures, and properties | Describe objects in context of a situation using geometric shapes | |

G.GMD.4 Identify the shapes of two dimensional cross sections of three dimensional objects, and identify three dimensional objects generated by rotations of two dimensional objects.

G.MG.1 Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).★

G.MG.3 Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).★

3D Figures

10.2 Develop and apply volume formulas

| | 4 – Mastery | 3 – Proficient | 2 - Basic | 1 – Below Basic | 0 – No Evidence |
|---|--|---|--|---|--|
| <p>Use Shapes and apply density concepts (G.MG.1, G.MG.2) Solve design problems (G.MG.3)</p> | <p>Can extend thinking beyond the standard, including tasks that may involve one of the following:</p> <ul style="list-style-type: none"> • Designing • Connecting | <p>Describe objects in context of a situation using geometric shapes and use them to solve problems related to</p> <ul style="list-style-type: none"> • <u>density based</u> on area and volume • design problems (ie. maximum volume, minimum cost, etc.) | <p>Describe objects in context of a situation using geometric shapes and use them to solve problems related to</p> <ul style="list-style-type: none"> • area and volume • <u>design problems</u> | <p>Describe objects in context of a situation using geometric shapes and use them to solve problems related to</p> <ul style="list-style-type: none"> • <u>area and volume</u> | <p>Little evidence of reasoning or application to solve the problem</p> <p>Does not meet the criteria in a level 1</p> |
| <p>Explain Formulas (G.GMD.1)</p> <p>Use Volume Formulas (G.GMD.3)</p> | <ul style="list-style-type: none"> • Synthesizing • Applying • Justifying • Critiquing • Analyzing • Creating • Proving | <p>Explain the formulas for <u>all of the following</u></p> <ul style="list-style-type: none"> • volume of a cylinder • volume of a pyramid • volume of a cone <p>using dissection arguments, cross sections of three dimensional objects, and Cavalieri’s principle</p> <p>Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems in context of a situation.</p> | <p>Explain the formulas for <u>2 of the following</u></p> <ul style="list-style-type: none"> • volume of a cylinder • volume of a pyramid • volume of a cone <p>using dissection arguments, cross sections of three dimensional objects, and Cavalieri’s principle</p> <p>Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems <u>in context of a situation.</u></p> | <p>Explain the formulas <u>for 1 of the following</u></p> <ul style="list-style-type: none"> • volume of a cylinder • volume of a pyramid • volume of a cone <p>using dissection arguments, cross sections of three dimensional objects, and Cavalieri’s principle</p> <p><u>Use volume formulas</u> for cylinders, pyramids, cones, and spheres to solve problems</p> | |

G.MG.1 Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).★

G.MG.2 Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).★

G.MG.3 Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).★

G.GMD.1 Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. Use dissection arguments, Cavalieri’s principle, and *informal limit arguments*.

G.GMD.2 (+) Give an informal argument using Cavalieri’s principle for the formulas for the volume of a sphere and other solid figures.

G.GMD.3 Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.★